



THE UNIVERSITY *of* EDINBURGH

## Edinburgh Research Explorer

### **Pecuniary Externality through Credit Constraints: Two Examples without Uncertainty**

**Citation for published version:**

Hardman-Moore, J 2013 'Pecuniary Externality through Credit Constraints: Two Examples without Uncertainty' ESE Discussion Papers, no. 233, Edinburgh School of Economics Discussion Paper Series.

**Link:**

[Link to publication record in Edinburgh Research Explorer](#)

**Document Version:**

Publisher's PDF, also known as Version of record

**Publisher Rights Statement:**

© Hardman-Moore, J. (2013). Pecuniary Externality through Credit Constraints: Two Examples without Uncertainty. (pp. 1-18). Edinburgh School of Economics Discussion Paper Series.

**General rights**

Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

**Take down policy**

The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact [openaccess@ed.ac.uk](mailto:openaccess@ed.ac.uk) providing details, and we will remove access to the work immediately and investigate your claim.





Edinburgh School of Economics  
**Discussion Paper Series**  
Number 233

*Pecuniary Externality through Credit Constraints:  
Two Examples without Uncertainty*

**John Moore**  
(Edinburgh University and LSE)

Date  
October 2013

***Published by***  
School of Economics  
University of Edinburgh  
30 -31 Buccleuch Place  
Edinburgh EH8 9JT  
+44 (0)131 650 8361  
<http://edin.ac/16ja6A6>



THE UNIVERSITY *of* EDINBURGH

Pecuniary Externality through Credit Constraints:

Two Examples without Uncertainty\*

by

John Moore

Edinburgh University and London School of Economics

October 2013

\*I thank Hans Gersbach, Nobuhiro Kiyotaki, Guido Lorenzoni and Jean-Charles Rochet for their thoughtful comments, and I am particularly grateful to Jordi Gali for his encouragement to write up these two examples. The examples arose from opportunities I had to discuss Gersbach and Rochet's paper "Aggregate Investment Externalities and Macro-Prudential Regulation" at a JMCB conference held in the Studienzentrum, Gerzensee, Switzerland, 20-21 October 2011, and to discuss Lorenzoni's paper "Inefficient Credit Booms" at a Research Workshop on the Economics of Financial Stability held in the Oesterreichische Nationalbank, Vienna, Austria, 7-8 July 2008.

## **ABSTRACT**

This paper is a contribution to the growing literature on constrained inefficiencies in economies with financial frictions. The purpose is to present two simple examples, inspired by the stochastic models in Gersbach-Rochet (2012) and Lorenzoni (2008), of deterministic environments in which such inefficiencies arise through credit constraints. Common to both examples is a pecuniary externality, which operates through an asset price. In the second example, a simple transfer between two groups of agents can bring about a Pareto improvement.

In a first best economy, there are no pecuniary externalities because marginal productivities are equalised. But when agents face credit constraints, there is a wedge between their marginal productivities and those of the non-credit-constrained agents. The wedge is the source of the pecuniary externality: economies with these kinds of imperfections in credit markets are not second-best efficient. This is akin to the constrained inefficiency of an economy with incomplete markets, as in Geanakoplos and Polemarchakis (1986).

## INTRODUCTION

This paper is a contribution to the growing literature on second-best inefficiencies in economies with financial frictions.<sup>1</sup> My purpose is to present two examples of *deterministic* environments in which pecuniary externalities arise through credit constraints.

The first example is inspired by Gersbach-Rochet (2012). I simplify and modify their stochastic model to show that the second-best inefficiency they identify is present in a two-period environment without uncertainty. The welfare measure I use to demonstrate constrained inefficiency is aggregate surplus – for which, of course, it is easier to exhibit a welfare improvement than if, say, the Pareto criterion were used.

The second example is inspired by Lorenzoni (2008). I simplify and modify his stochastic model to show that uncertainty is not necessary to his analysis. But here the welfare criterion I use is more demanding: I demonstrate that a simple transfer between two groups of agents can bring about a Pareto improvement.

Common to both examples is a *pecuniary* externality, which operates through an asset price. In a first best economy, we know that there are no pecuniary externalities because marginal productivities are equalised. But in both my examples, certain agents face credit constraints. On account of these credit constraints, there is a wedge between their marginal productivities and those of the non-credit-constrained agents. The wedge is the source of the pecuniary externality: economies with these kinds of imperfections in credit markets are not even second-best efficient. This is akin to the constrained inefficiency of an economy with incomplete markets. See, for example, Geanakoplos and Polemarchakis (1986).

---

<sup>1</sup> See, for example, Lorenzoni (2008), Jeanne and Korinek (2010), Korinek (2011), Davila (2012), Gersbach and Rochet (2012), He and Kondor (2012), Hart and Zingales (2013), Jeanne and Korinek (2013). For papers that are of a more dynamic stochastic general equilibrium (DSGE) nature, see, for example, Bianchi and Mendoza (2010), Jeanne and Korinek (2010). There are also papers on exchange rate externalities as opposed to asset price externalities; see, for example, Caballero and Krishnamurthy (2003), Korinek (2011). At the intersection of DSGE and exchange rate externalities, see, for example, Bianchi (2011).

## EXAMPLE 1

There are two days, 0 and 1, and two groups of agents, sheep farmers and wine makers. Production occurs overnight, between days 0 and 1. Consumption is on day 1. The agents' respective outputs, wool and wine, are perfect substitutes as consumption goods. Measuring them so as to be one-for-one in consumption, we can take wool and wine to be a common unit of account, "output", the numeraire.

Besides their own non-tradable labour, sheep farmers and wine makers both use land as an input to production. Land can be traded on day 0, in exchange for a promise to deliver day 1 output, wool or wine. But – and this is the key to the model – the promise has to be credible. The only trade in this economy is the exchange of land on day 0 for a credible promise to deliver day 1 output.

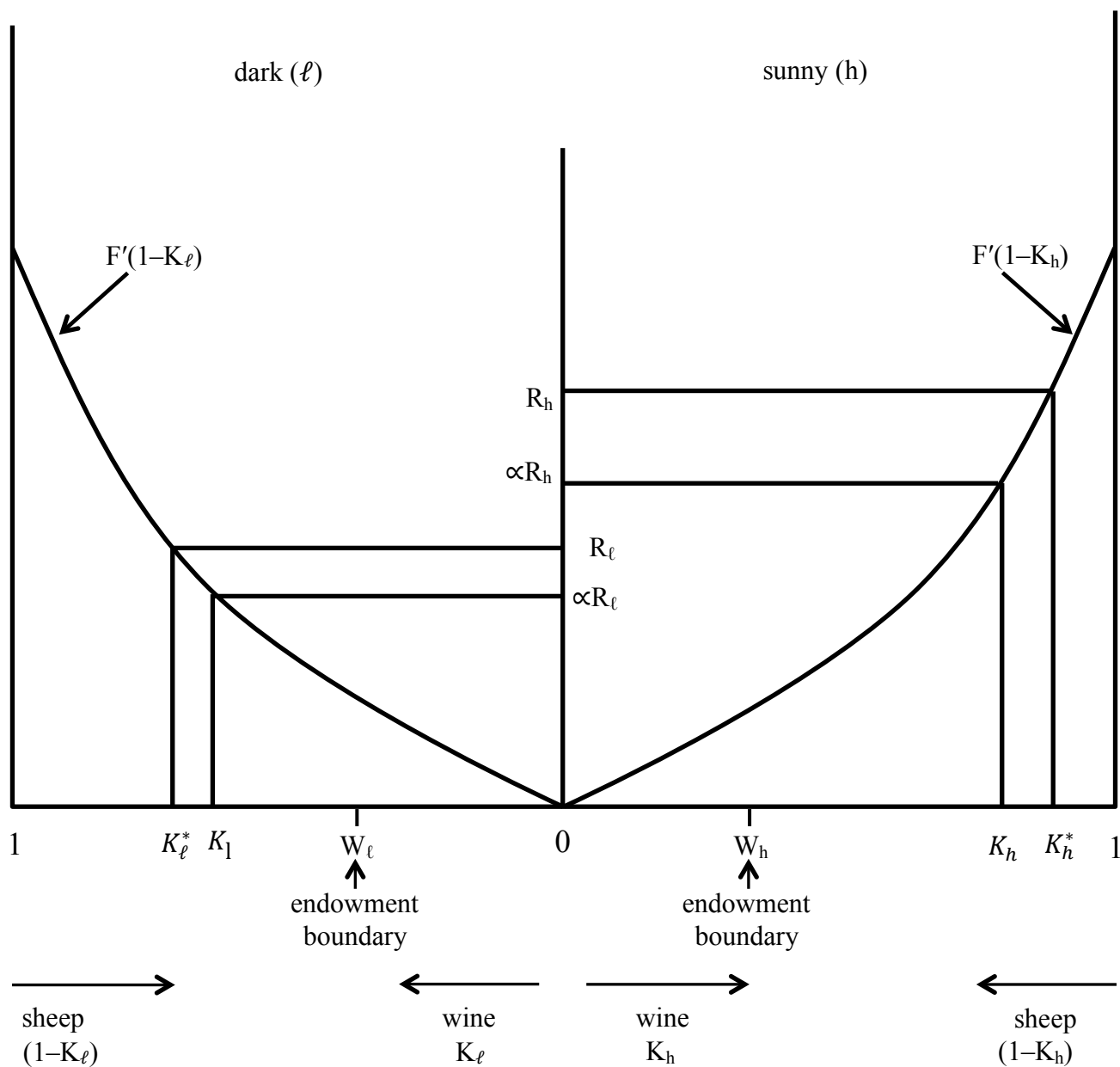
Land is variably productive. Think of land in thin contours, or strips, in a valley whose cross-section has the shape of an inverted Gothic arch; see Figure 1. Along each contour, parallel to the valley floor, the land is at a constant altitude and is homogeneous. Take the overall width of the valley, perpendicular to the valley floor, to be 2, and suppose the altitude (above sea-level, not the valley floor) of a contour horizontal distance  $K$  from the valley floor is given by the constant elasticity function

$$\eta(a + 1 - K)^{\eta-1} \quad \text{where } a > 0 \text{ and } 0 < \eta < 1.$$

Productivity – both for sheep rearing and vine growing measured per (tiny) unit-width strip – varies across strips. It can depend on the altitude of the strip as well as on which side of the valley the strip is on.

On the dark side of the valley, the left side of Figure 1, the sun seldom shines and so the productivity of growing vines is less than on the right, the sunny side. But the productivity of growing vines is *not* affected by altitude: it is a constant,  $R_\ell > 0$ , on the left; and a constant,  $R_h > R_\ell$ , on the right.

Rearing sheep *is* affected by altitude – sheep thrive in higher altitudes – but is unaffected by light. Supposing that productivity is a *linear* function of altitude, we can measure altitude so as to make them equal. Thus, for example, if all the land on one side of



productivity of vine growing { increasing with light  
unaffected by altitude

productivity of sheep rearing { increasing with altitude (equal to!)  
unaffected by light

Figure 1

the valley, above a contour horizontal distance  $K$  from the valley floor, were devoted to sheep rearing, then output from this land would be

$$(a + 1 - K)^\eta - a^\eta \equiv F(1 - K), \text{ say.}$$

The derivative,  $F'(1 - K)$ , of this function is the altitude  $\eta(a + 1 - K)^{\eta-1}$  – equal to the productivity of rearing sheep – of a strip horizontal distance  $K$  from the valley floor.

Crucially, on day 0 wine makers can credibly pledge at most a fraction  $\theta < 1$  of their day 1 output. We will see that, because of this, they face a “credit constraint”. (Note that we could also assume, for symmetry, that on day 0 sheep farmers too are unable to credibly pledge more than a fraction  $\theta$  of their day 1 output, but that would not substantively affect our analysis. So let us not make this assumption.)

Wine makers are endowed with all the lowest strips of land, horizontal distance up to  $W_\ell$  from the valley floor on the dark side, and up to  $W_h$  on the sunny side. Sheep farmers are endowed with all the remaining land. The values of  $W_\ell$  and  $W_h$  are small enough that at the boundaries, the productivity of sheep rearing is strictly less than  $\theta$  times that of wine making:

$$F'(1 - W_\ell) < \theta R_\ell$$

and

$$F'(1 - W_h) < \theta R_h.$$

### 1.1. Implementation of the First-Best

The initial endowment of land is not too inefficient: the higher land (land more productive for sheep rearing) belongs to the sheep farmers; and the lower land (land more productive for vine growing) belongs to the wine makers. But to reach first-best requires equating productivities at the boundaries on each side of the valley:

$$F'(1 - K_\ell^{\text{FB}}) = R_\ell$$



and

$$F'(1 - K_h^{FB}) = R_h$$

where  $K_\ell^{FB}$  is the horizontal distance from the valley floor, in the first-best allocation, of the boundary between sheep rearing and vine growing on the dark side of the valley, and  $K_h^{FB}$  is similarly defined for the sunny side.

As a preliminary observation: implementation of this first-best allocation can be decentralised as a market equilibrium outcome if  $\theta$  is equal to 1, so that wine makers face no credit constraint.

Market equilibrium pricing, in the first-best when  $\theta$  equals 1, is as follows. On the dark side of the valley, all strips of land up to horizontal distance  $K_\ell^{FB}$  from the valley floor are uniformly priced at  $R_\ell$ ; each higher strip, horizontal distance  $K > K_\ell^{FB}$  from the valley floor, is priced at  $F'(1 - K)$ . And on the sunny side, all strips of land up to horizontal distance  $K_h^{FB}$  from the valley floor are uniformly priced at  $R_h$ ; each higher strip, horizontal distance  $K > K_h^{FB}$  from the valley floor, is priced at  $F'(1 - K)$  – as on the dark side.

The point is that, when  $\theta$  equals 1, competition drives the land price up to the zero-profit level across the valley.

## 1.2. Laissez faire equilibrium with credit constraints

When the wine makers' credit constraint binds (requiring that  $\theta < 1$ ), the nature of the land pricing is similar. On the dark side of the valley, for some  $P_\ell$ , land horizontal distance up to  $K_\ell$  from the valley floor is priced at  $P_\ell$ , where  $K_\ell$  solves

$$F'(1 - K_\ell) = P_\ell;$$

and each higher strip, horizontal distance  $K > K_\ell$  from the valley floor, is priced at  $F'(1 - K)$ . And on the sunny side, for some  $P_h$ , land horizontal distance up to  $K_h$  from the valley floor is priced at  $P_h$ , where  $K_h$  solves

$$F'(1 - K_h) = P_h;$$

and each higher strip, horizontal distance  $K > K_h$  from the valley floor, is priced at  $F'(1 - K)$ .

Sheep farmers compete to buy all the higher land, the land priced above  $P_\ell$  and  $P_h$  on the dark and sunny sides respectively. They make zero profit.

The equilibrium values of  $P_\ell$  and  $P_h$  are determined by the behaviour of the wine makers. We will see that, in equilibrium, wine makers use more land than their aggregate endowment; i.e.  $K_\ell > W_\ell$  and  $K_h > W_h$ .

Consider a typical wine maker, endowed with land worth  $y$ . (The argument is the same whichever side of the valley his endowment lies: it may be  $y/P_\ell$  units on the dark side, or  $y/P_h$  units on the sunny, or a convex combination. He can realise  $y$  by selling his endowment and then investing in land either on the dark or sunny side of the valley.) If he invests on the dark side, the scale of his investment  $k$  will be governed by a flow-of-funds constraint

$$P_\ell k \leq y + \theta R_\ell k,$$

given that he cannot credibly pledge more than a fraction  $\theta$  of his day 1 return  $R_\ell k$ . His day 1 net payoff is maximised when the constraint binds. That is, his maximum payoff from levered investment on the dark side of the valley is

$$\frac{(1 - \theta)R_\ell y}{P_\ell - \theta R_\ell}$$

By a similar argument, his maximum payoff from levered investment on the sunny side of the valley is

$$\frac{(1 - \theta)R_h y}{P_h - \theta R_h}$$

In equilibrium, these rates of return on levered investment must be equalized (so as to have vine growing on both sides of the valley):

$$\frac{(1 - \theta)R_\ell}{P_\ell - \theta R_\ell} = \frac{(1 - \theta)R_h}{P_h - \theta R_h}$$

Here the denominators are the downpayments required per unit of land purchased; the numerators are the output that cannot be pledged.

It follows from this equation that there must exist some  $\alpha$  such that

$$P_\ell = \alpha R_\ell$$

and

$$P_h = \alpha R_h$$

Note that  $\alpha$  is strictly greater than  $\theta$  (the required downpayments are positive). And  $\alpha$  is strictly less than 1 (the rates of return on levered investment exceed 1).

### 1.3 Planner's constrained optimum

Think now of a planner choosing  $K_\ell$  and  $K_h$  to maximise aggregate output

$$R_\ell K_\ell + F(1 - K_\ell) + R_h K_h + F(1 - K_h)$$

subject to the constraint

$$[K_\ell - W_\ell]F'(1 - K_\ell) + [K_h - W_h]F'(1 - K_h) \leq \theta R_\ell K_\ell + \theta R_h K_h$$

The logic here is that, in choosing  $K_\ell$  and  $K_h$ , the planner is in effect choosing prices  $P_\ell = F'(1 - K_\ell)$  and  $P_h = F'(1 - K_h)$ . The planner's problem is constrained by the need to

respect the (aggregate of the) wine makers' credit constraints, assuming that they and the sheep farmers take  $P_\ell$  and  $P_h$  as parametric prices.

Form the Lagrangian  $L$ , with multiplier  $\lambda$ . The first-order conditions (FOCs) are:

$$\begin{aligned}\frac{\partial L}{\partial K_\ell} &= R_\ell - F'(1 - K_\ell) - \lambda \{F'(1 - K_\ell) - [K_\ell - W_\ell]F''(1 - K_\ell) - \theta R_\ell\} \\ &= 0\end{aligned}$$

$$\begin{aligned}\frac{\partial L}{\partial K_h} &= R_h - F'(1 - K_h) - \lambda \{F'(1 - K_h) - [K_h - W_h]F''(1 - K_h) - \theta R_h\} \\ &= 0\end{aligned}$$

The solution,  $(K_\ell^{SB}, K_h^{SB})$  say, to these FOCs are the second-best values of  $K_\ell$  and  $K_h$  – the constrained efficient allocation of land across sheep rearing and vine growing.

#### 1.4 Constrained inefficiency of laissez-faire

To compare these values  $K_\ell^{SB}$  and  $K_h^{SB}$  with the laissez-faire equilibrium

$$\begin{cases} F'(1 - K_\ell) = \alpha R_\ell \\ F'(1 - K_h) = \alpha R_h \end{cases}$$

we substitute these values of  $K_\ell$  and  $K_h$  into the left-hand sides of the above first-order conditions:

$$\frac{1}{R_\ell} \frac{\partial L}{\partial K_\ell} = 1 - \alpha - \lambda \left\{ \alpha - \theta + \left[ \frac{K_\ell - W_\ell}{1 - K_\ell} \right] \alpha (1 - \eta) \right\}$$

and

$$\frac{1}{R_h} \frac{\partial L}{\partial K_h} = 1 - \alpha - \lambda \left\{ \alpha - \theta + \left[ \frac{K_h - W_h}{1 - K_h} \right] \alpha (1 - \eta) \right\}$$

The crucial point is that, typically, these expressions for  $\frac{\partial L}{\partial K_\ell}$  and  $\frac{\partial L}{\partial K_h}$  cannot *both* be equal to zero, because typically

$$\left[ \frac{K_\ell - W_\ell}{1 - K_\ell} \right] \neq \left[ \frac{K_h - W_h}{1 - K_h} \right]$$

Thus, typically, *the laissez-faire equilibrium does not maximise aggregate output subject to the wine makers' credit constraints*. The laissez-faire equilibrium is typically not constrained efficient.

For example, in the special case where  $W_\ell = W_h$ , since  $K_\ell < K_h$ ,

$$\frac{\partial L}{\partial K_h} < 0 < \frac{\partial L}{\partial K_\ell}$$

– evaluated at the allocation of the laissez-faire equilibrium with credit constraints. In this special case, relative to this laissez-faire allocation, the planner wants to raise  $K_\ell$  (raise  $P_\ell$ ) and lower  $K_h$  (lower  $P_h$ ). With  $W_\ell = W_h$ , a small increase in the price  $P_\ell$ , offset by an equal reduction in the price  $P_h$ , makes no difference to the wine makers' (credit-constrained) aggregate output, but shifts a little sheep rearing from the less productive boundary on the dark side of the valley, productivity  $F'(1 - K_\ell)$ , to the more productive boundary on the sunny side of the valley, productivity  $F'(1 - K_h)$ .

The disparity between the planner's second-best allocation and the laissez-faire allocation arises because the planner internalises the effect his choice of  $K_\ell^{SB}$  and  $K_h^{SB}$  has on the prices  $P_\ell$  and  $P_h$ , whereas the market does not. Absent the wine makers' credit constraint, and the resultant wedge between their productivity and the marginal productivity of the sheep rearers – i.e., in the first-best – this would not matter. But it *does* matter in the second-best.

## EXAMPLE 2

The example follows the model in Lorenzoni (2008), but with important differences, which will be pointed out.

There are three dates,  $t = 0, 1, 2$ , and two types of agent, entrepreneurs and consumers. There is a consumption good, fruit, that is perishable, and a capital good that perishes at  $t = 2$ . Unlike in Lorenzoni (2008), there is no uncertainty. And, critically, there is no financial contracting, because there is no collateral available to secure borrowing.

Start with a representative entrepreneur. At  $t = 0$ , he is endowed with  $n$  units of fruit, but thereafter he has no endowment. He can convert fruit into capital, one-for-one:  $k_0$  capital held overnight between  $t = 0$  and  $t = 1$  yields him  $ak_0$  fruit at  $t = 2$  (not at  $t = 1$  as in Lorenzoni (2008)), where  $a > 1$ . Neither capital nor fruit have collateral value, hence no borrowing is possible. The entrepreneur will choose to invest all his endowment in capital:  $k_0 = n$ .

At  $t = 1$ , the capital stock requires maintenance (otherwise it perishes), using up  $\gamma k_0$  fruit, where  $\gamma < 1$ . Hence the entrepreneur needs to raise funds, by selling  $k_0 - k_1$  newly-maintained capital, at price  $q$  (in terms of fruit), where  $\gamma < q < 1$ .  $k_1$  units of capital held overnight between  $t = 1$  and  $t = 2$  yields him again  $Ak_1$  fruit at  $t = 2$ , where  $A > 1$ . Given that there is no borrowing, the maintenance costs have to be wholly met from asset sales:

$$\gamma k_0 = q(k_0 - k_1)$$

or

$$k_1 = (q - \gamma)k_0/q$$

At  $t = 2$ , the entrepreneur eats fruit  $ak_0 + Ak_1$ , his utility.

Now turn to a representative consumer. She has a large endowment of fruit at each date  $t = 0, 1$  and  $2$ . She eats fruit  $c_t$  each date: her utility is  $c_0 + c_1 + c_2$ . She can also produce fruit by holding capital overnight between  $t = 1$  and  $t = 2$ : in aggregate,  $k_0 - k_1$

capital acquired by consumers at  $t = 1$  yields  $F(k_0 - k_1)$  fruit at  $t = 2$ . Specifically, we suppose

$$F(k_0 - k_1) \equiv 2(k_0 - k_1)^{1/2}$$

The first-order conditions for (non-discounted) profit maximisation:

$$F'(k_0 - k_1) = q$$

imply that at  $t = 1$  the consumers' demand for capital,  $k_0 - k_1$ , equals  $1/q^2$  and that their maximised profit (utility),  $\pi$ , from fruit production equals  $1/q$ .

## 2.1. Equilibrium

In the market for capital at  $t = 1$ :

$$\text{supply} = \gamma k_0 / q$$

$$\text{demand} = 1 / q^2$$

Notice that the supply schedule is a downward-sloping function of the price. However the demand schedule is less steeply downward-sloping, which ensures that the equilibrium is unique and stable. See Figure 2.

The competitive equilibrium price  $q$  is

$$q^{\text{CE}} = 1 / \gamma k_0$$

which equals  $1 / \gamma n$  given that the entrepreneurs choose  $k_0 = n$  at  $t = 0$ .

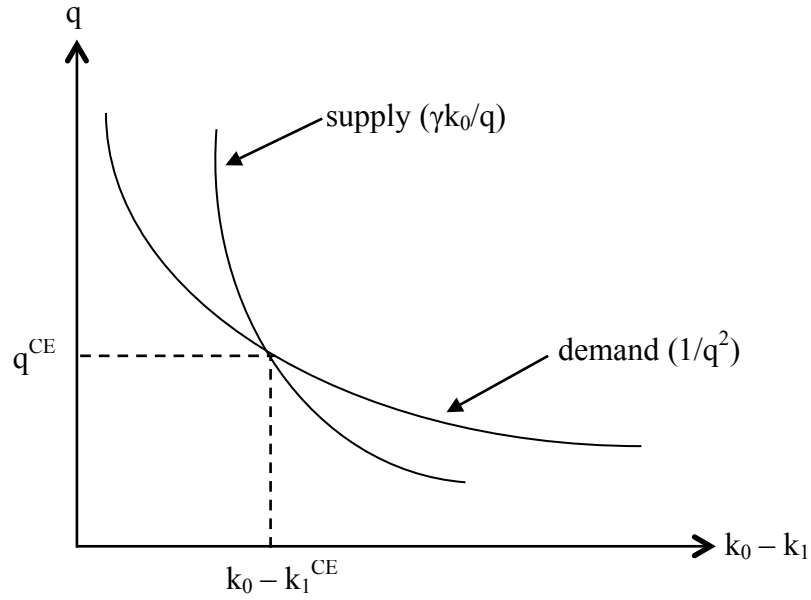


Figure 2

The price  $q^{CE}$  lies strictly between  $\gamma$  and 1 if we assume:

$$1/\gamma < n < 1/\gamma^2 \quad (\text{Assumption 1})$$

In equilibrium, the consumer profit  $\pi$  is

$$\pi^{CE} = 1/q = \gamma k_0,$$

which equals  $\gamma n$  given  $k_0 = n$ . And the entrepreneurs' capital holding  $k_1$  between  $t = 1$  and  $t = 2$  is

$$k_1^{CE} = (q - \gamma)k_0 / q = (1 - \gamma^2 k_0)k_0,$$



which, given  $k_0 = n$ , equals  $(1 - \gamma^2)n$ . This is positive by Assumption 1.

We suppose that maintenance costs  $\gamma k_0$  are large enough that, in the neighbourhood of  $n$ , a fall in  $k_0$  would lead to a *rise* in  $k^{CE}$ . Specifically, we assume

$$\gamma > 1/\sqrt{2n} \quad \text{or} \quad 1/2\gamma^2 < n \quad (\text{Assumption 2})$$

Assumption 2 ensures that

$$k_1^{CE} = (1 - \gamma^2 k_0)k_0$$

would go *up* if  $k_0$  went down. Note that Assumptions 1 and 2 are compatible. They can be amalgamated:

$$\max\{1/\gamma, 1/2\gamma^2\} < n < 1/\gamma^2$$

## 2.2. Welfare

Consider the following experiment. At  $t = 0$ , suppose the entrepreneurs are obliged to transfer a small amount of fruit,  $\tau_0 = \varepsilon$ , to the consumers.

As a result, the entrepreneurs' capital investment  $k_0$  is reduced by  $\varepsilon$  – down from  $n$  to  $n - \varepsilon$ :

$$\Delta k_0 = -\varepsilon < 0.$$

This reduction in  $k_0$  lowers the entrepreneurs' maintenance costs  $\gamma k_0$  at  $t = 1$ , shifts down their capital supply schedule in the market, and hence raises the equilibrium price  $q^{CE}$  from  $1/\gamma n$  to  $1/\gamma(n - \varepsilon)$ :

$$\Delta q \approx \varepsilon / \gamma n^2 > 0.$$

The price rise reduces the consumers' profit  $\pi^{CE}$  from  $\gamma n$  to  $\gamma(n - \varepsilon)$ :

$$\Delta \pi = -\gamma \varepsilon < 0,$$

but, since  $\gamma < 1$ , the consumers are more than compensated by the initial payment  $\tau_0 = \varepsilon$ . And the entrepreneurs' capital holding  $k_1^{CE}$  between  $t = 1$  and  $t = 2$  rises from  $(1 - \gamma^2 n)n$  to  $(1 - \gamma^2 n + \gamma^2 \varepsilon)(n - \varepsilon)$ :

$$\Delta k_1 \approx (2\gamma^2 n - 1)\varepsilon,$$

which is strictly positive by Assumption 2. The effect on the entrepreneurs' consumption (utility) at  $t = 2$  is

$$a\Delta k_0 + A\Delta k_1 \approx -a\varepsilon + A(2\gamma^2 n - 1)\varepsilon,$$

which is strictly positive if  $A$  is enough larger than  $a$ . Specifically, we assume

$$A / a > 1 / (2\gamma^2 n - 1) \quad (\text{Assumption 3})$$

Here, the right hand side is strictly greater than 1 given Assumptions 1 and 2. Hence Assumption 3 implies  $A > a$ .

Under Assumptions 1-3, then, the consumers *and* the entrepreneurs are strictly better off as a result of the experiment. We have a strict Pareto improvement!

### 2.3. Intuition for the Pareto improvement

Between  $t = 1$  and  $t = 2$ , the entrepreneurs' return on fruit equals

$$A / q > 1$$

whereas consumers' (marginal) return on fruit only equals

$$F'(k_0 - k_1) / q = 1$$

This differential in returns reflects the entrepreneurs' borrowing constraint at  $t = 1$ . *Ceteris paribus*, it would therefore be efficient to inject funds (fruit) into the hands of the entrepreneurs at  $t = 1$ .

Unfortunately, consumers cannot commit at  $t = 0$  to pay anything to the entrepreneurs at  $t = 1$ : in effect the consumers, too, cannot "borrow" at  $t = 0$  because they have no collateral. Also, the entrepreneurs cannot store (perishable) fruit between  $t = 0$  and  $t = 1$ .

However, there is an indirect method of injecting funds. Namely, raise the price  $q$  of capital sold by the entrepreneurs at  $t = 1$  – by reducing  $k_0$ , so as to lower their maintenance costs  $\gamma k_0$  and thus shift down their capital supply schedule.

Individually, an entrepreneur cannot raise the price  $q$ , and so will not choose to reduce his private choice of capital investment at  $t = 0$ . But, collectively, the rise in  $q$  helps all entrepreneurs.

The price rise directly hurts the consumers, but the transfer of fruit at  $t = 0$  more than compensates.

Via  $ak_0$ , the reduction in  $k_0$  directly hurts the entrepreneurs' consumption at  $t = 2$ ; but this is more than made up for via  $Ak_1$  and the increase in  $k_1$ , provided  $A$  is enough larger than  $a$ .

Everyone is strictly better off. This strict Pareto improvement is implemented through a simple transfer  $\tau_0$  from the entrepreneurs to the consumers at  $t = 0$ .

## 2.4. Summary

It may be worthwhile summing up example 2. Consider the effect on the group of entrepreneurs,  $E$ , of an upfront transfer from them to the group of consumers,  $C$ . The scale of group  $E$ 's ex ante investment is reduced, which reduces their maintenance costs, thus reducing their need to sell assets at the interim date. The market-clearing asset price rises, which indirectly helps all group  $E$ : in effect, funds are injected at the interim date from group  $C$  to group  $E$ . The gain, to group  $E$ , from this injection of funds through the raised asset price, can outweigh their direct loss from the transfer. Meantime, group  $C$  indirectly loses from the rise in asset price, but this can be more than offset by their direct gain from the transfer. Overall, everyone can be a net gainer: the ex ante transfer can lead to a Pareto improvement.

Notice the somewhat paradoxical nature of the transfer: *from* the credit-constrained group  $E$  *to* the unconstrained group  $C$ . One might have expected the direction to be the other way: from the deep pockets (group  $C$ ) to the shallow pockets (group  $E$ ). The reason why the upfront transfer from group  $E$  to group  $C$  works well is that it facilitates an indirect subsidy back from group  $C$  to group  $E$  at the crucial interim date when, at the margin, disinvestment by group  $E$  is socially inefficient: group  $E$ 's return on retaining a marginal unit of asset can greatly exceed the return to group  $C$ .

At the heart of this there lies a tension between the individual and the group. No *individual* entrepreneur would choose to curtail his ex ante investment, because he is too small to affect the asset price at the interim date. As a *group*, however, the entrepreneurs are better off if they reduce their ex ante investment – thereby, at the interim date, reducing their maintenance costs and raising the asset price.

## REFERENCES

- Bianchi, Javier, and Enrique Mendoza, 2010, Overborrowing, Financial Crises, and 'Macroprudential' Taxes, NBER Working Paper w16091.
- Bianchi, Javier, 2011, Overborrowing and Systemic Externalities in the Business Cycle, *American Economic Review* 101(7).
- Caballero, Ricardo J., and Arvind Krishnamurthy, 2003, Excessive Dollar Borrowing: Financial Development and Underinsurance, *Journal of Finance* 58(2).
- Davila, Eduardo, 2012, Dissecting Fire Sales Externalities, Harvard, mimeo.
- Geanakoplos, John and Heraklis Polemarchakis, 1986, Existence, Regularity, and Constrained Suboptimality of Competitive Allocations when the Asset Market Is Incomplete, in Walter Heller, Ross Starr, and David Starrett (eds.), *Essays in Honor of Kenneth Arrow*, Vol. 3. Cambridge University Press, 1986, pp. 65-95.
- Gersbach, Hans and Jean-Charles Rochet, 2012, Aggregate Investment Externalities and Macroprudential Regulation, Swiss Finance Institute Research Paper 12-03.
- Hart, Oliver and Luigi Zingales, 2013, Liquidity and Inefficient Investment, NBER Working Paper No. 19184.
- He, Zhiguo and Peter Kondor, 2012, Inefficient Investment Waves, NBER Working Paper No. 18217.
- Jeanne, Olivier and Anton Korinek, 2010, Excessive Volatility in Capital Flows: A Pigouvian Taxation Approach, *American Economic Review* 100(2).
- Jeanne, Olivier, and Anton Korinek, 2010, Managing Credit Booms and Busts: A Pigouvian Taxation Approach, NBER Working Paper w16377.
- Jeanne, Olivier, and Anton Korinek, 2013, Macroprudential Regulation versus Mopping Up After the Crash, NBER Working Paper w18675.
- Korinek, Anton, 2011, The New Economics of Prudential Capital Controls, *IMF Economic Review* 59(3).
- Korinek, Anton, 2011, Systemic Risk-Taking: Amplification Effects, Externalities, and Regulatory Responses, ECB Working Paper 1345.
- Lorenzoni, Guido, 2008, Inefficient Credit Booms, *Review of Economic Studies* 75(3).